

# Algorithmic trading

Bruno Biais (TSE) & Thierry Foucault (HEC)

May 2010

# Outline

- 1) Definition and typology of algos
- 2) Theoretical considerations on algos
  - Algos & limited cognition
  - Algos & adverse selection
  - Algos & moral hazard
  - Algos & systemic risk
- 3) Empirical evidence
- 4) Conclusion

# 1) Algos

Computers collect & process info faster than humans => trade on it

Even when humans not present or actively monitoring (no human intervention)

# What do they do?

Determine which assets to trade	Trade fast on news  Identify & exploit arb or investment opportunities
Predefined choice of assets	Work orders  Consume or supply liquidity  Search for best execution

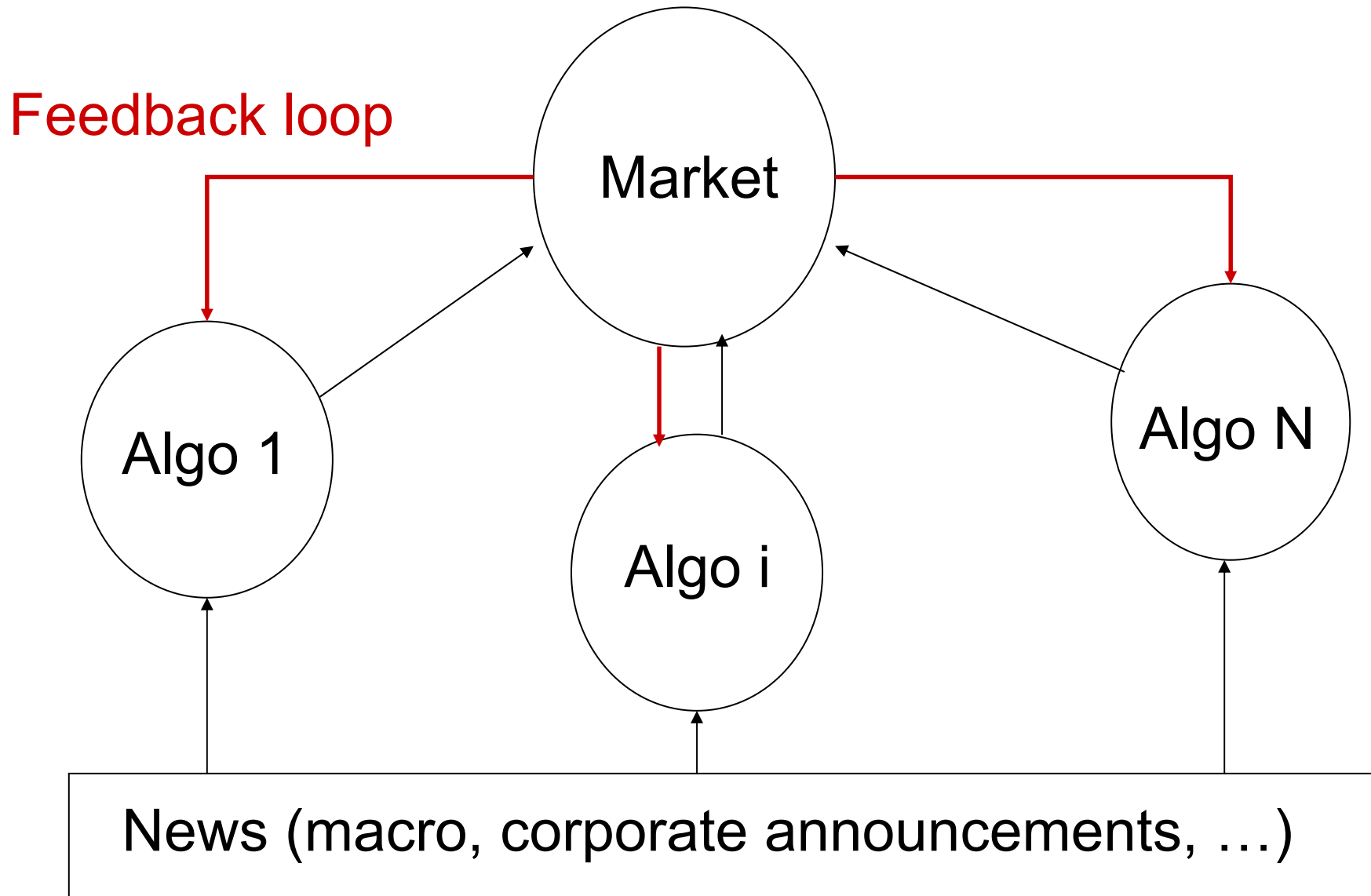
# Who uses them?

Determine which assets to trade	Trade fast on news  Identify & exploit opportunities	→ Prop traders Hedge funds
Predefined choice of assets	Work orders  Consume or supply liquidity  Search for best execution	→ Prop traders Hedge funds Brokers

# What info do they use?

Determine which assets to trade	Trade fast on news Identify & exploit opportunities	Info about market (depth & quotes) & common value of asset
Predefined choice of assets	Work orders Consume or supply liquidity Search for best execution.	Info about market (depth & quotes) & private value of trader

# Algos, traders & markets



## 2) Theory



# What are the pros & cons of algos?

Perfect market => algos don't matter

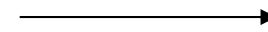
What market imperfections?

i) Limited cognition

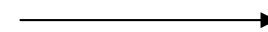
ii) Moral hazard

iii) Adverse selection

iv) Systemic risk



pros



cons

# With limited cognition algos improve gains from trade

Without algos, information collection & processing delays slow down order placement & matching of buyers and sellers (with different private values)

Algos enhance order placement opportunities & improve speed and quality of matching

=> greater gains from trade, more liquidity

=> market more resilient to shocks

=> less transient volatility in prices

=> greater informational efficiency

# “Limited cognition, liquidity shocks & order book dynamics”

Biais, Hombert & Weill (2010)

Market hit by aggregate liquidity shock transiently reducing willingness to hold asset of all traders.

Traders emerge from distress at random times: when they do, they recover high valuation for asset.

Efficient allocation of asset to high valuation traders hindered by limited cognition: It takes time for traders to evaluate their own position (have they emerged from stress?) & design optimal strategies.

Algos reduce delay on investors' trades => improve efficiency of allocation/gains from trades => liquidity.

With limited cognition algos  
improve speed at which info is  
incorporated into prices

Without algos, information collection &  
processing delays slow down incorporation  
of new information in quotes & prices

Algos enhance ability of traders to digest and  
express info  
=> greater informational efficiency

# Algos & agency problems

Moral hazard: actions of agents not observable

Example: Is broker really providing best execution?

Algorithm: search for price & execution strategy of broker **observable**

- => mitigates agency problem
- => reduces rents for brokers, costs for investors
- => facilitates delegation & reliance on more sophisticated strategies (dynamics, splitting, multi-market, etc...)
- => market effectively more liquid & transactions less costly for final investors

# Algos can reduce adverse selection for liquidity suppliers

Foucault, Roell, Sandas, Review of Financial Studies (2003)

Algos => fast electronic monitoring of market

If liquidity suppliers use fast algos

=> they face less adverse selection

=> spreads tighten & liquidity improves

=> price discovery enhanced too, as quotes more  
informative

# Algos can also increase adverse selection for liquidity suppliers

If fast algo traders use market orders to hit slow limit orders, this worsens adverse selection for the limit order traders

=> spread widens & liquidity supply lower

# Algos & information asymmetry

There is information about (common) value of assets waiting out there to be used

Algos get it faster than the others

=> Information asymmetry between algos & others

=> Trading profits for algos / costs for others

Prices informationally efficient a little bit faster, but slow investors more reluctant to participate in market => lower gains from trade & liquidity



# Level playing field?

High fixed cost of algos

- => develop computer program, hire specialists
- => buy fast connection to exchange servers  
(co-location)

Large traders fast, small traders slow

- => small traders face adverse selection
- => compete less aggressively to supply liquidity
- => liquidity supply less competitive
- => spreads widen / depth decline

# Algos & systemic risk

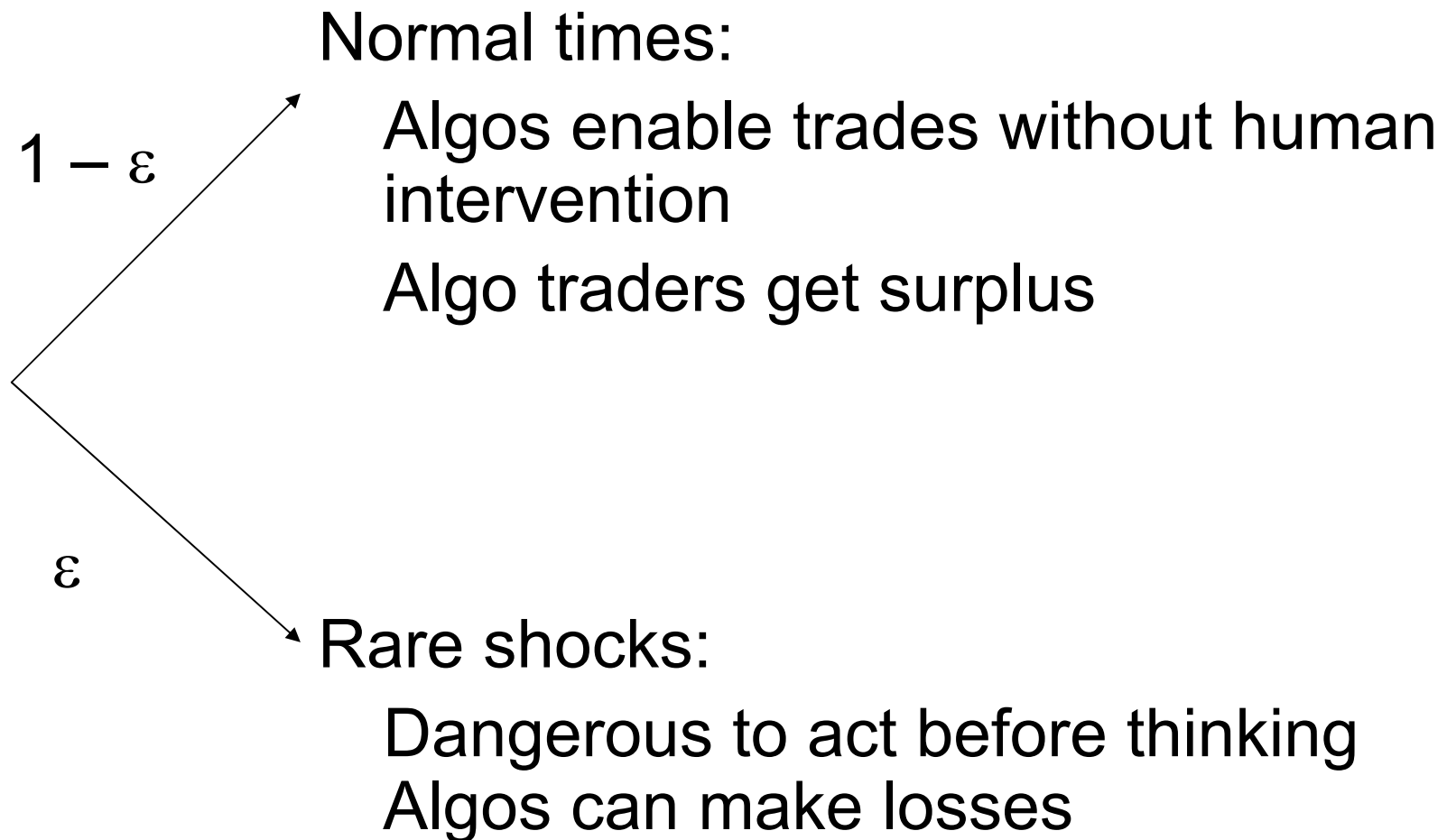
Normal times: algo trades not too correlated/not too big in aggregate => don't move prices too much.

Algos designed to trade optimally in this context.

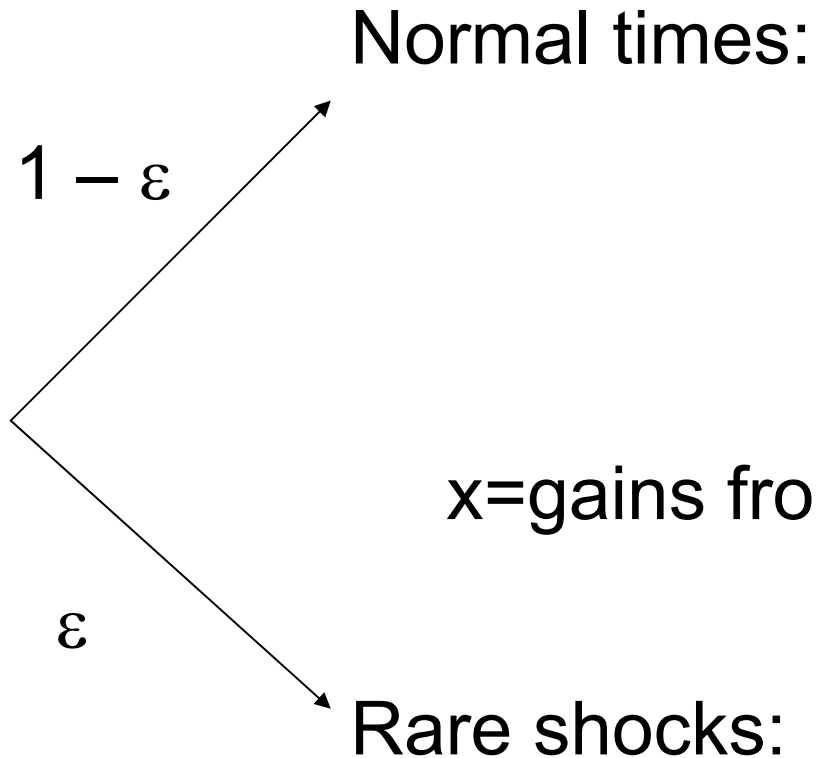
Rare shocks: exceptional/sudden increase in correlation between algos => aggregate algo trade big => push price.

Algos react fast & automatically to this price movement (without taking time to think about its exceptional nature) => push price further => spiral.

# A simple synthetic model of pros & cons



## 2 trading environments



1 \ 2	Fast	Slow
Fast	x,x	y,-y
Slow	-y,y	0,0

x=gains from trade, y= private info rent

1 \ 2	Fast	Slow
Fast	-L,-L	-L,0
Slow	0,-L	0,0

L = loss from action without human intervention under exceptional circumstances

# Utilitarian social welfare

If both fast =  $2 [(1-\varepsilon) x - \varepsilon L]$

If one fast, the other slow =  $-\varepsilon L$

If both slow = 0

Fast is socially optimal if  $\varepsilon$  and  $L$  low and  $x$  high:

$$(1-\varepsilon) x > \varepsilon L$$

Otherwise slow is socially optimal

# Equilibrium when $\varepsilon=0$

1 \ 2	Fast	Slow
Fast	$x, x$	$x+y, x-y$
Slow	$-y, y$	$0, 0$

$E(\text{profit} | \text{I am fast, the other is fast}) = x$

$E(\text{profit} | \text{I am fast, the other is slow}) = y$

$E(\text{profit} | \text{I am slow, the other is fast}) = -y$

$E(\text{profit} | \text{I am slow, the other is slow}) = 0$

Fast = dominant strategy: enables to reach gains from trade, and avoids informational disadvantage.

# Equilibrium when $\varepsilon > 0$

$$E(\text{profit} | \text{I am fast, the other is fast}) = (1-\varepsilon) x - \varepsilon L$$

$$E(\text{profit} | \text{I am fast, the other is slow}) = (1-\varepsilon) y - \varepsilon L$$

$$E(\text{profit} | \text{I am slow, the other is fast}) = (1-\varepsilon) (-y)$$

$$E(\text{profit} | \text{I am slow, the other is slow}) = 0$$

Fast = Nash equilibrium if

$$(1-\varepsilon) (x+y) > \varepsilon L$$

Slow = Nash equilibrium if

$$(1-\varepsilon) y < \varepsilon L$$

# Inefficient equilibrium

If

$$(1-\varepsilon) y > \varepsilon L > (1-\varepsilon) x$$

Fast = unique symmetric pure Nash equilibrium

This equilibrium is socially suboptimal

Prisoners' dilemma: algos socially suboptimal,  
but if others use algos I must do the same.



## 3) Empirical evidence

# “Does Algorithmic Trading Improve Liquidity?”

Hendershott, Menkveld & Jones  
Forthcoming Journal of Finance

Proxy for algo trading: ratio of messages (orders, cancels, modifications, etc...) to volume

Instrument: start of autoquoting on NYSE

Finding: For large-cap stocks, quoted and effective spreads & informativeness of quotes increase.

But realized spreads increase: rents for the (smaller number of) liquidity suppliers who became fast.

# “Algorithmic Trading and Information”

Hendershott & Riordan, 2010

Algorithmic trades, 30 DAX stocks, Deutsche Börse.

AT liquidity demand (market orders) = 52% of volume

Algos supply liquidity on 50% of volume.

Algos monitor the market for liquidity & deviations of price from fundamental value.

Algos consume liquidity when it is cheap and supply liquidity when it is expensive.

AT contributes to efficiency by placing efficient quotes & trading to move towards efficient price.

# “Rise of the Machines: Algorithmic Trading in the Foreign Exchange Market”

Chaboud, Chiquoine, Hjalmarsson, Vega 2010

Interdealer trading in currency market 2006 2007

Algo trades correlated

No causal relationship between algo trading & volat

Algos less active in the minute following macro releases, but algos supply liquidity over the hour following release

# “What happened to the quants in August 2007?” Khandani & Lo, 2010

August 6, 2007: Hedge funds/prop traders hit by shock from credit market

⇒margin calls & reduction in position limits

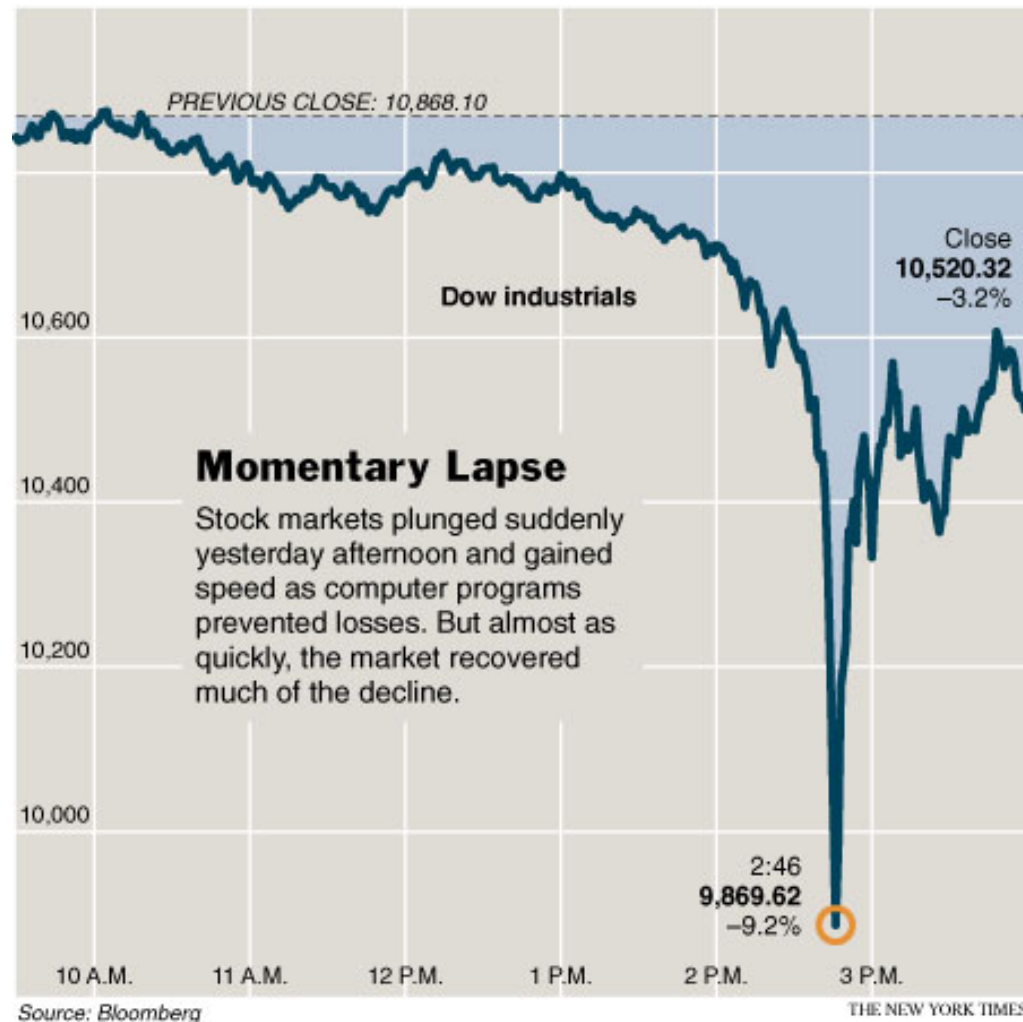
⇒fast unwinding in equity market

⇒push price down: spiral

August 10, 2007: market recovers.

These quantitative funds processed lots of data => used algos: Was the spiral due to algos? Would it happen without algos? Was it worsened by algos?

# What happened on May 7 2010?



Was the 9% drop in the Dow due to spiral of algos?

## 4) Conclusion

# Conclusion: What do we learn from theory?

Pros: Algos can help mitigating limited cognition & moral hazard problems, and thus improve liquidity & gains from trade.

Cons: But they can also reduce competition or increase systemic risk.

The cons are less clearly understood by theory than the pros



# Conclusion: What do we learn from empirical observations?

There are only a few studies, so far.

Econometric studies of normal times suggest that algos don't reduce liquidity & increase price efficiency.

Case studies of rare crisis suggests algos might worsen systemic risk.

Very little data available: need more data to conduct more systematic studies.

# Conclusion: preliminary & tentative policy implications

Co-location: creates potential information asymmetry,  
without obvious huge efficiency improvement

=> Regulation could improve liquidity by enforcing  
level playing field

Algos might be destabilizing in exceptional  
circumstances

=> High frequency monitoring by market organizers  
& trading halts (enforced across market venues)  
could provide useful safeguards