

Behavioral bias in number processing: Evidence from analysts' expectations

Séance du Conseil Scientifique
Autorité des Marchés Financiers (AMF)

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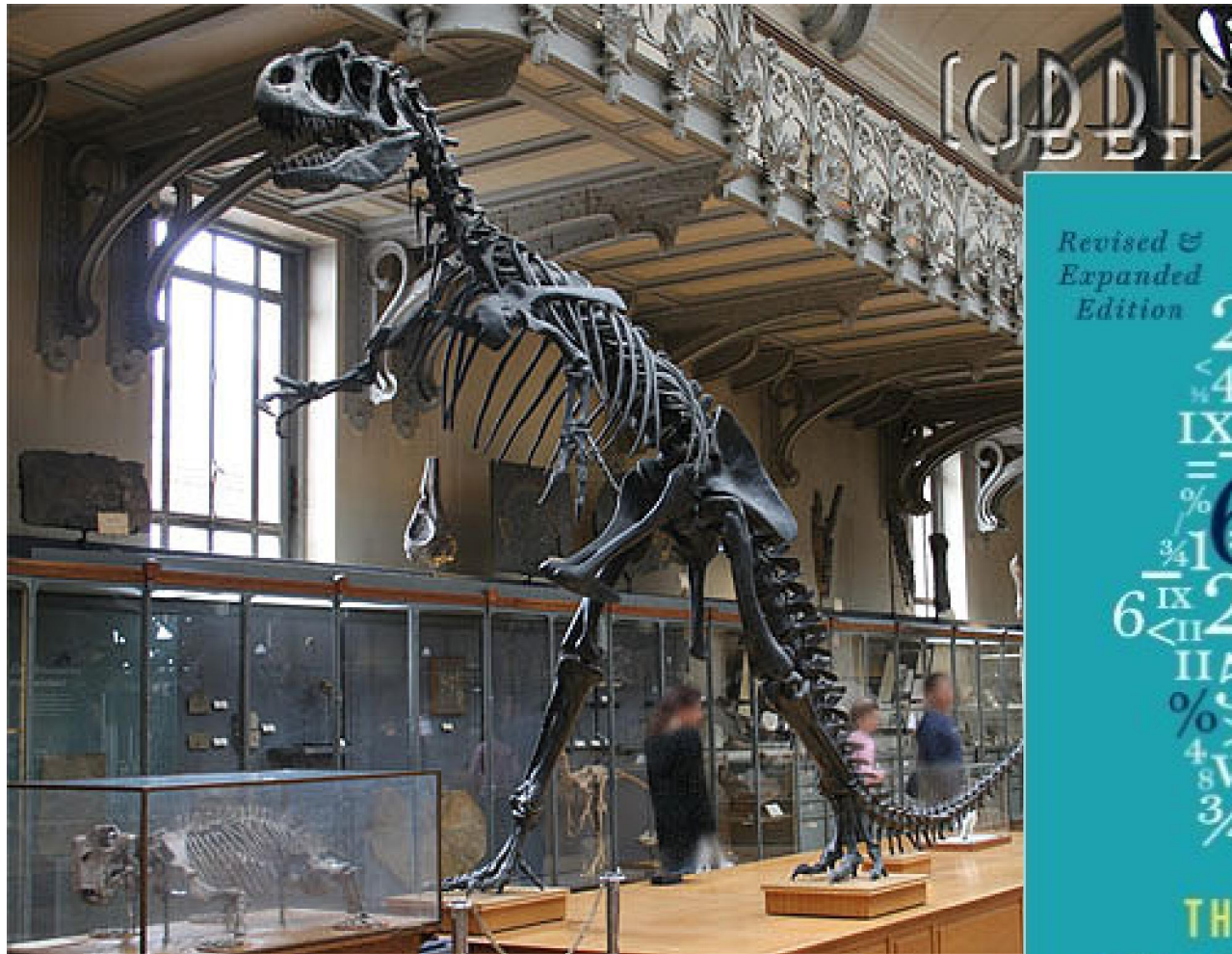
Paris, France

Tristan Roger

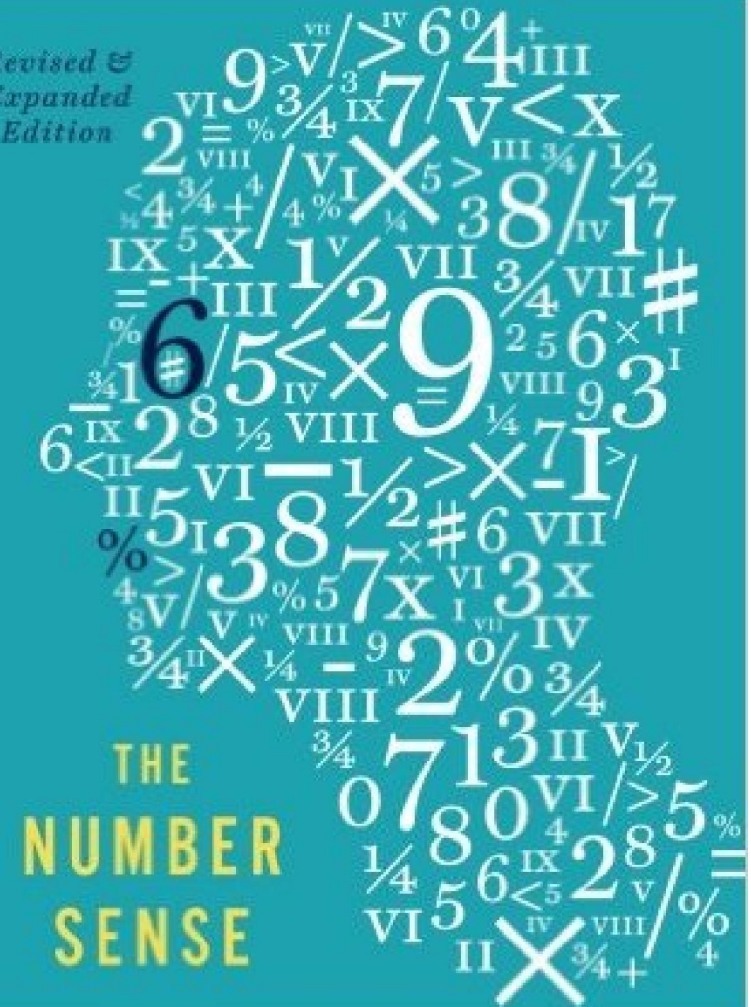
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Article co-écrit avec P. Roger et A. Schatt
R&R at *Journal of Economic Behavior and Organization*



Revised &
Expanded
Edition



THE NUMBER SENSE

[HOW THE MIND CREATES MATHEMATICS]

STANISLAS DEHAENE

Introduction

Database and
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statistics

Univariate analysis

Multivariate
analysis

Recommendations

Stock splits

Conclusion

Introduction

- The human brain processes numbers on a mental number line
 - Small numbers are represented on the left part of the line
 - Large numbers are represented on the right part of the line
 - The opposite is observed in cultures where people write from the right to the left

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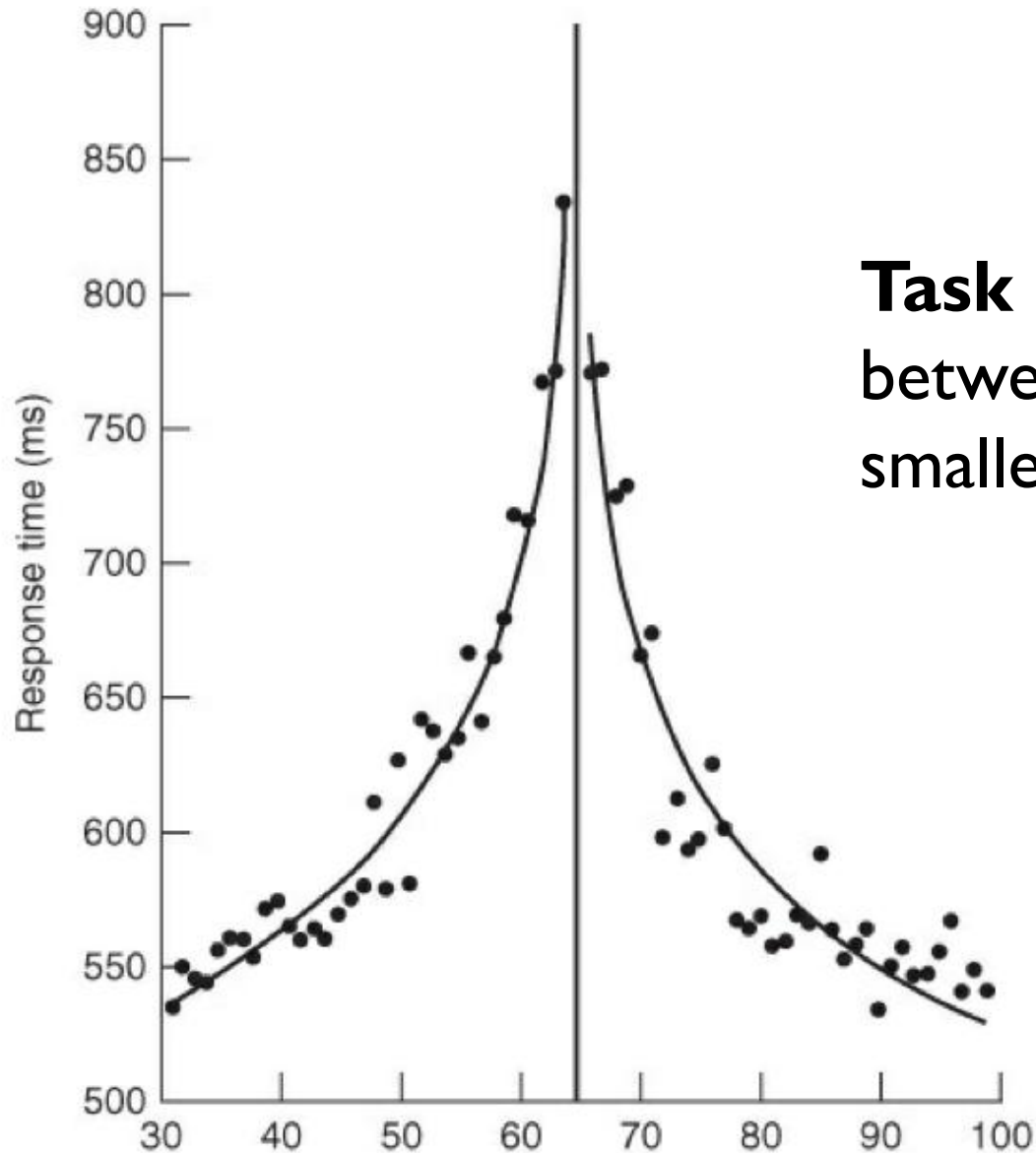
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- Number processing (Weber's law)
 - Distance effect
 - Faster to recognize that 10 is greater than 1 than to perceive that 6 is greater than 5

Illustration of the distance effect



Task : classify numbers between 31 and 99 as being smaller or larger than 65

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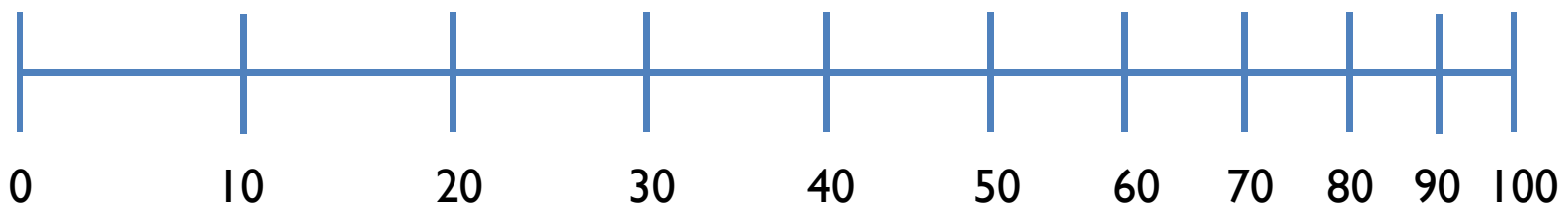
Introduction

- Number processing (Weber's law)
 - Distance effect
 - Faster to recognize that 10 is greater than 1 than to perceive that 6 is greater than 5
 - Size effect
 - Faster to recognize that 6 is greater than 5 than to perceive that 35 is greater than 34
- Numbers are processed by the brain on a logarithmic scale
 - Nieder (2005)
- Deviations from the logarithmic scale are observed for small numbers
 - Dehaene *et al.* (2008); Hyde and Spelke (2009)

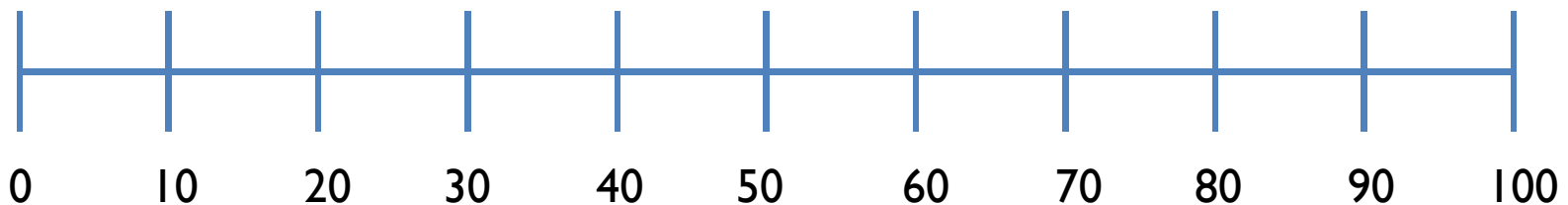
Introduction

- Number processing

- Logarithmic scale



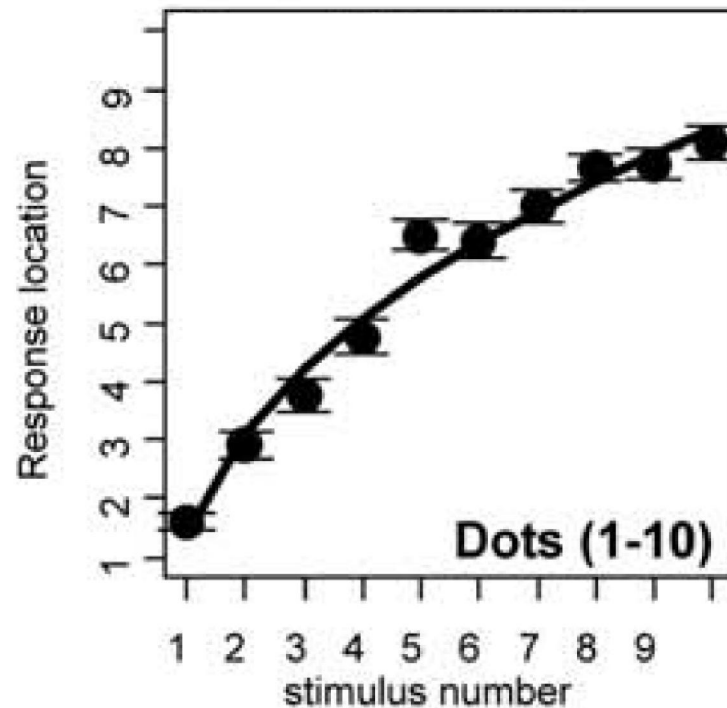
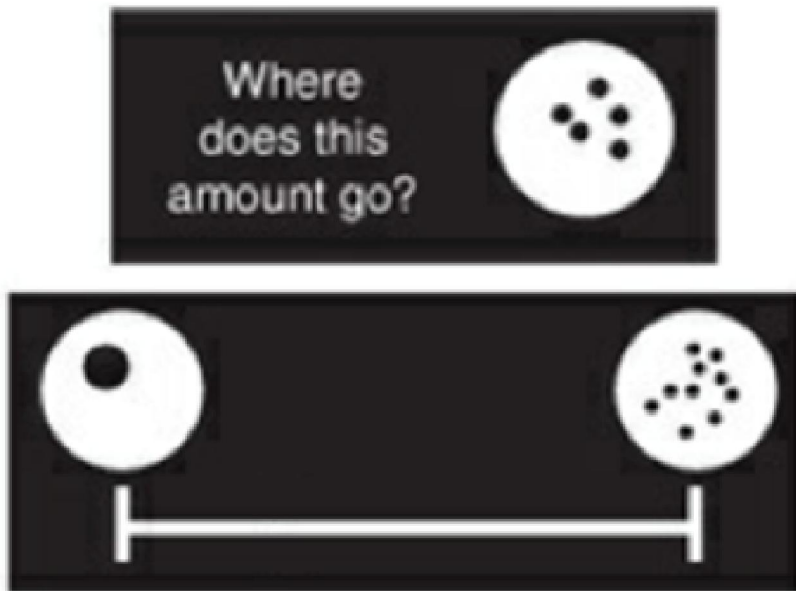
- Linear scale



- Education “linearizes” numerical distances (especially for small numbers)

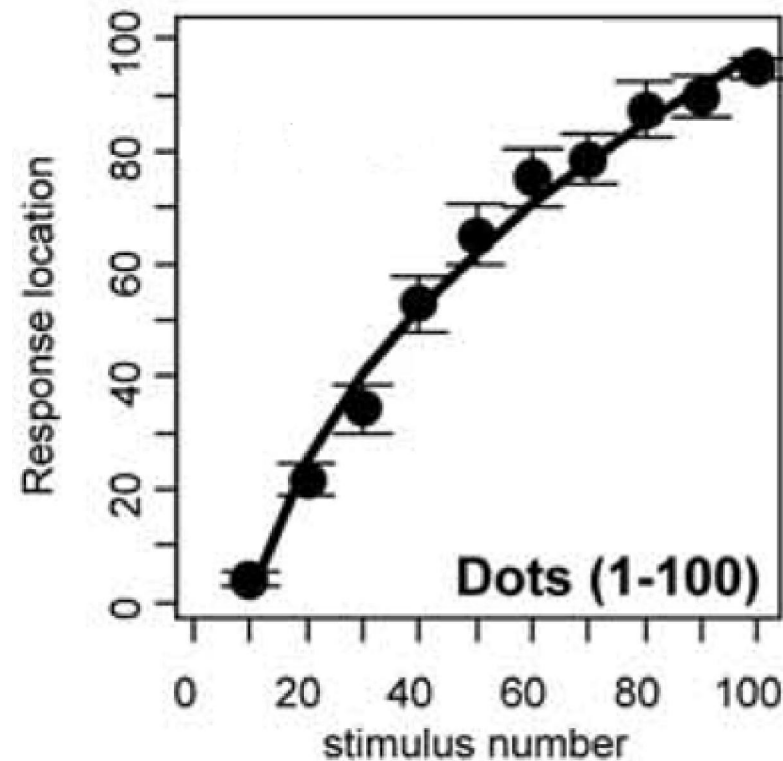
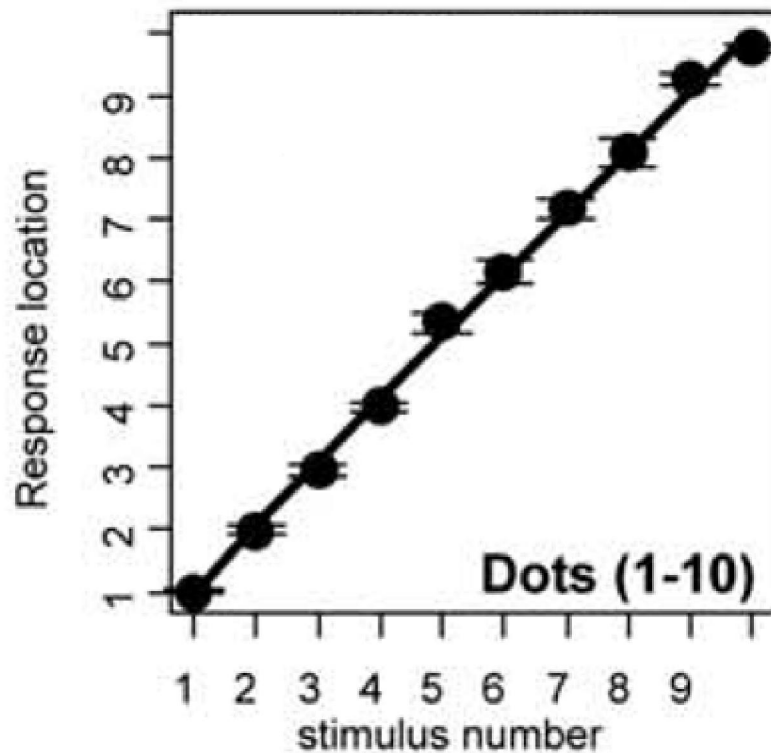
Introduction

- Results of an experiment on Mundurucu adults
 - Dehaene *et al.* (2008)
- Subjects are asked to locate numbers on a line



Introduction

- Results of an experiment on American adults (Dehaene *et al.*, 2008)
 - Subjects are asked to locate numbers on a line



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Introduction

- **Financial analysts**
 - ❑ Earnings forecasts
 - ❑ Recommendations
 - ❑ Target prices
 - Significant abnormal returns following target price revisions (both unconditional and conditional on contemporaneously issued recommendations and earnings forecast revisions)
 - Brav and Lehavy (2003), *Journal of Finance*
 - Asquith, Mikhail and Au (2005), *Journal of Financial Economics*

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- **Analysts' optimism bias**
 - **Conflicts of interest**
 - Incentives to produce inaccurate figures
 - Lim (2001)
 - Mehran and Stulz (2007)
 - Bradshaw, Huang and Tan (2014)
 - Jackson (2005)
 - **Behavioral biases**
 - Some heuristics lead analysts to miscalculate
 - Cen, Hilary and Wei (2013)

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- What is our paper about?
 - We evidence a specific behavioral bias
 - The small price bias
 - Analysts process small stock prices differently than large stock prices
 - Our paper is grounded in recent research in neuropsychology on number processing

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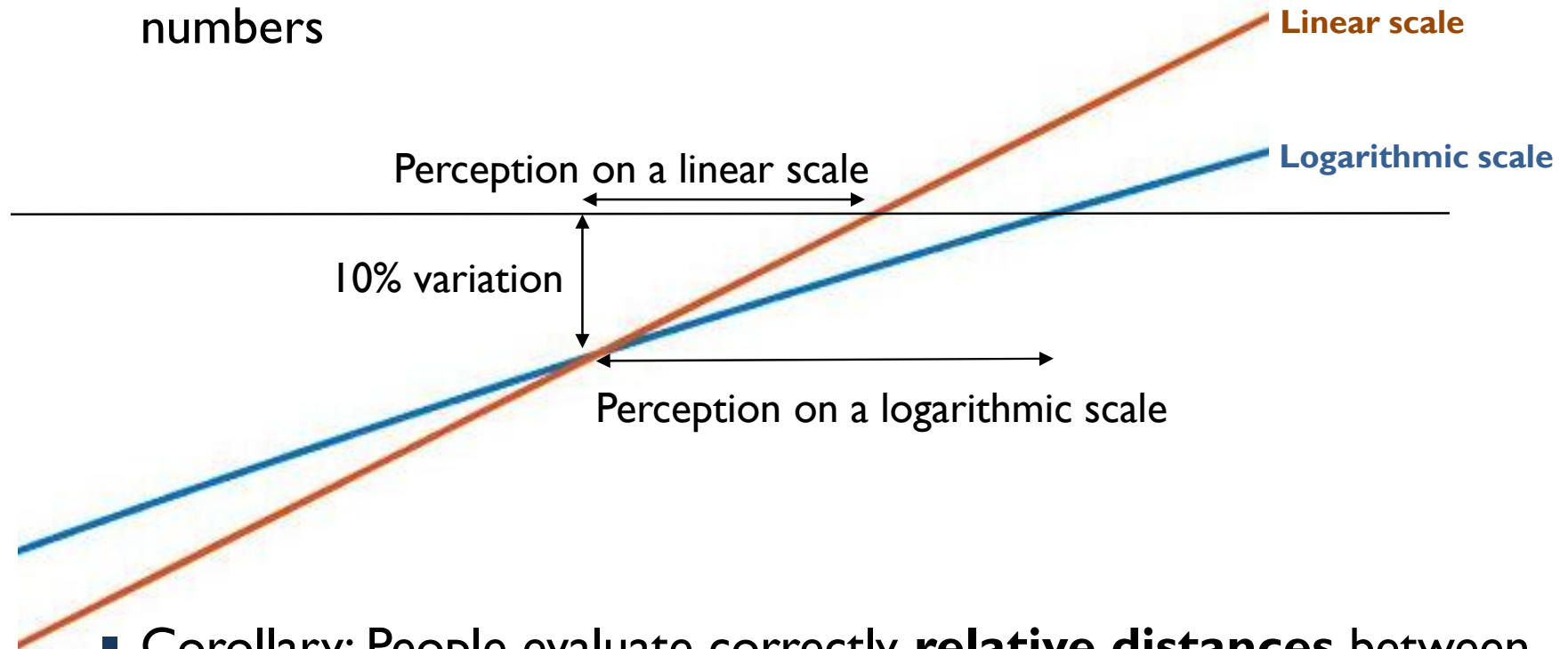
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Introduction

- Number processing - summing up
 - Individuals tend to use a linear scale for small numbers and a logarithmic scale for larger numbers
 - A price variation from \$3 to \$3.2 is seen as 20 cts increase
 - A price variation from \$101 to \$110 is seen (approximately) as a 10% increase (not a \$9 variation)
- Our hypothesis
 - If analysts use a linear scale for small price stocks and a logarithmic scale for large price stocks, they will provide more optimistic target prices for small price stocks than for large price stocks

Linear vs. Logarithmic

- People evaluate correctly **absolute distances** between small numbers but underrepresent **absolute distances** between large numbers



- Corollary: People evaluate correctly **relative distances** between large numbers but exaggerate **relative distances** between small numbers

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Data

- 2000-2013 period
- Data on target prices (I/B/E/S)
 - 814,117 target prices issued by 9,141 analysts on 6,423 stocks
- Data on stock prices (CRSP)
 - NYSE, AMEX, NASDAQ
 - Stock prices
 - Stock splits
- Market, size, book-to-market and liquidity factors (WRDS, Kenneth French's website)
- Data on recommendations (I/B/E/S)
- Compustat

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Descriptive statistics

	Number of target prices	Number of analysts	No. of analysts per firm	Proportion of optimistic target prices	Average implied return
2000	34,027	3,111	9.62	96.04%	37.89%
2001	39,466	3,428	11.41	93.64%	31.95%
2002	46,441	3,258	12.21	92.40%	29.09%
2003	48,109	2,657	11.13	84.40%	17.46%
2004	51,505	2,728	11.20	85.55%	17.17%
2005	52,049	2,785	10.87	86.46%	16.73%
2006	53,442	2,743	11.07	85.69%	16.57%
2007	56,504	2,730	11.34	86.83%	16.77%
2008	67,619	2,679	11.59	88.44%	27.82%
2009	65,544	2,603	12.76	82.22%	18.82%
2010	69,254	2,989	14.78	87.62%	18.52%
2011	76,180	3,044	15.57	89.11%	20.48%
2012	72,677	2,913	15.49	87.53%	18.95%
2013	81,300	2,781	16.03	83.43%	13.46%

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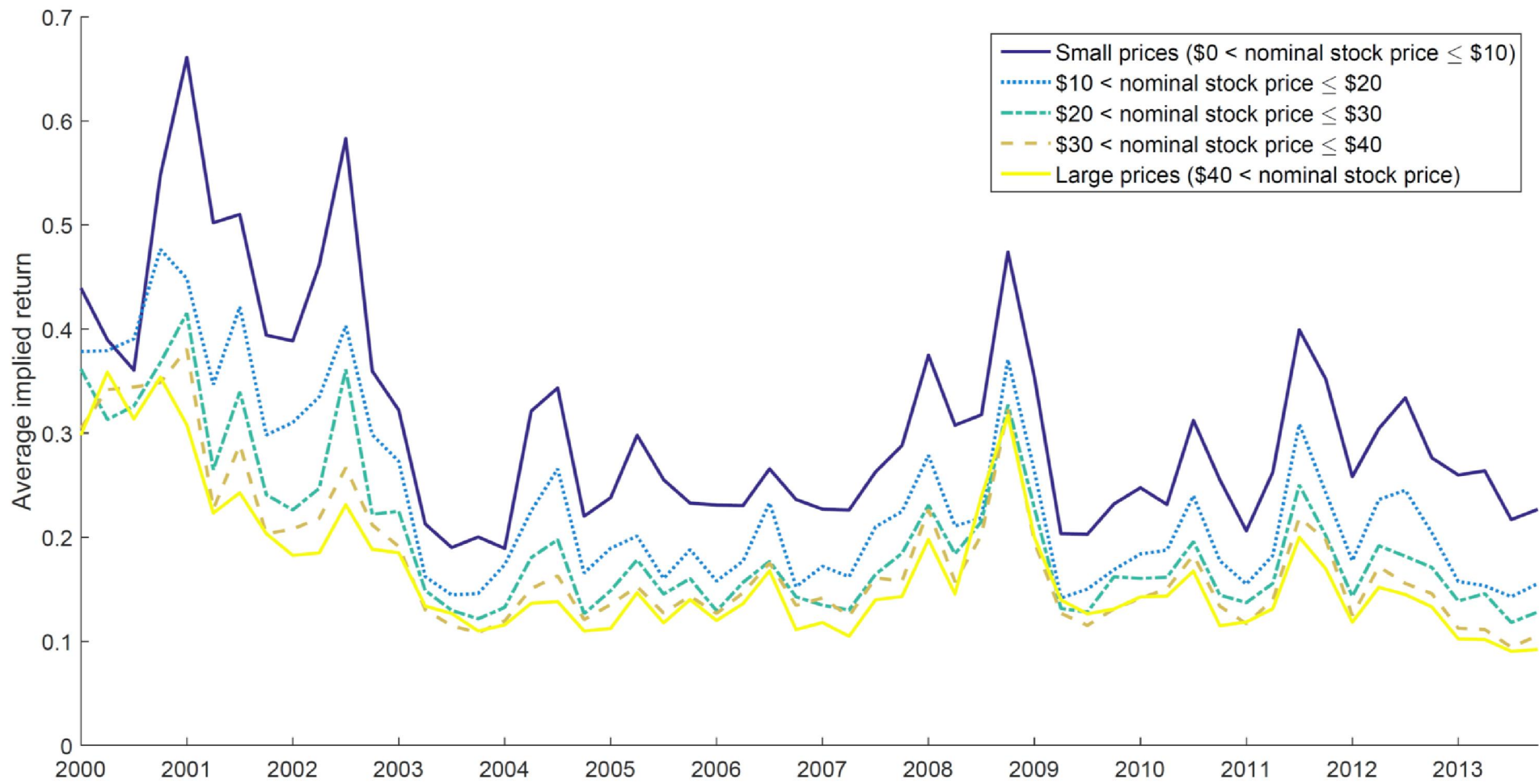
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Univariate analysis

- Stock prices and implied returns
 - We build five price categories
 - **Category 1:** stock prices between \$0 and \$10
 - **Category 2:** stock prices between \$10 and \$20
 - **Category 3:** stock prices between \$20 and \$30
 - **Category 4:** stock prices between \$30 and \$40
 - **Category 5:** stock prices above \$40
 - For each quarter between January 2000 and December 2013, we compute the average implied return for each price category

Univariate analysis



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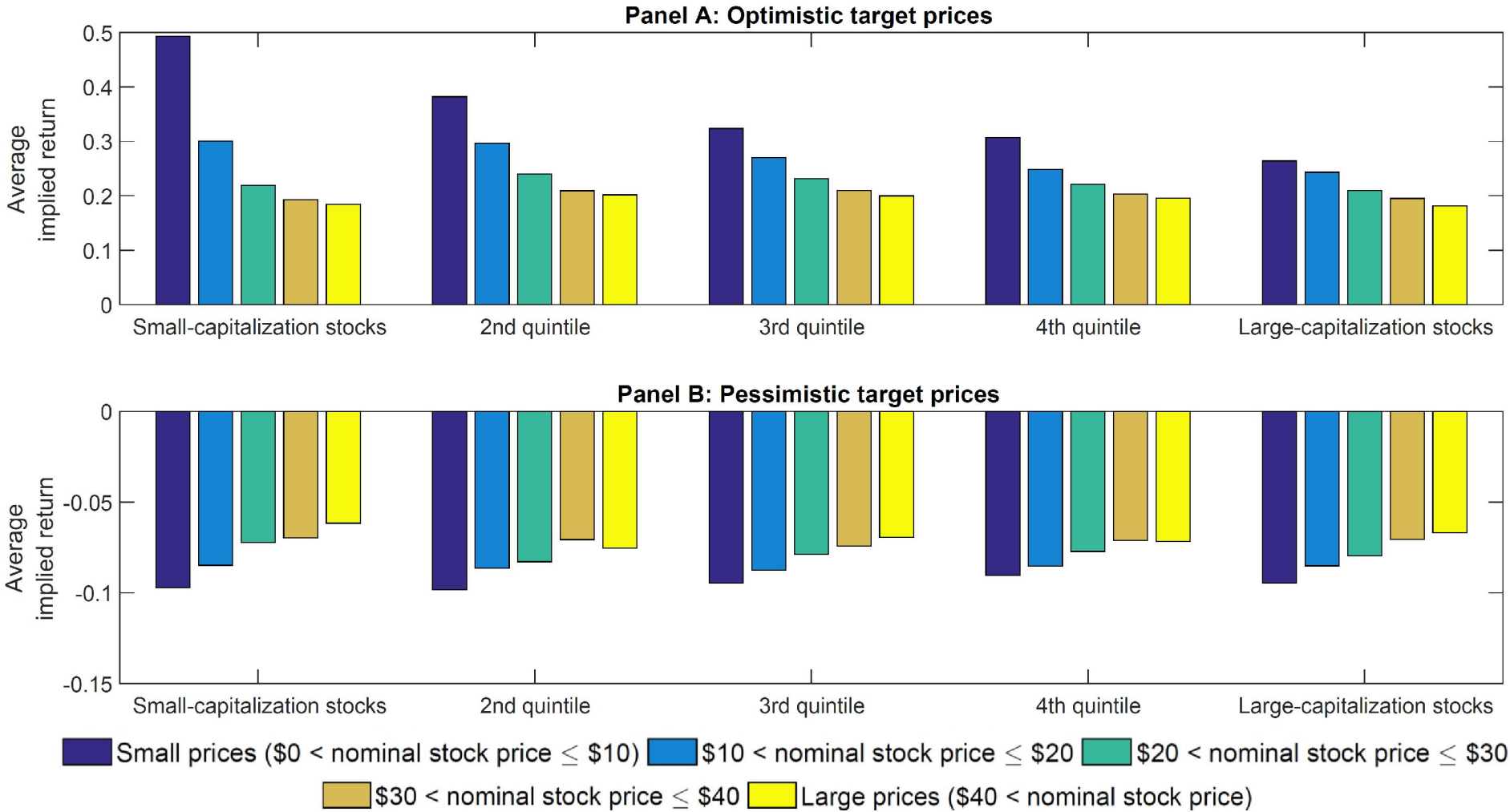
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Univariate analysis

- **Stock prices and market capitalization**
 - There exists a strong correlation between nominal prices and firm size
 - However, this correlation is not perfect due to
 - Choice of IPO price
 - Stock splits
 - Stock dividends
 - We use a double sort on nominal prices and market capitalization to disentangle size and price effects

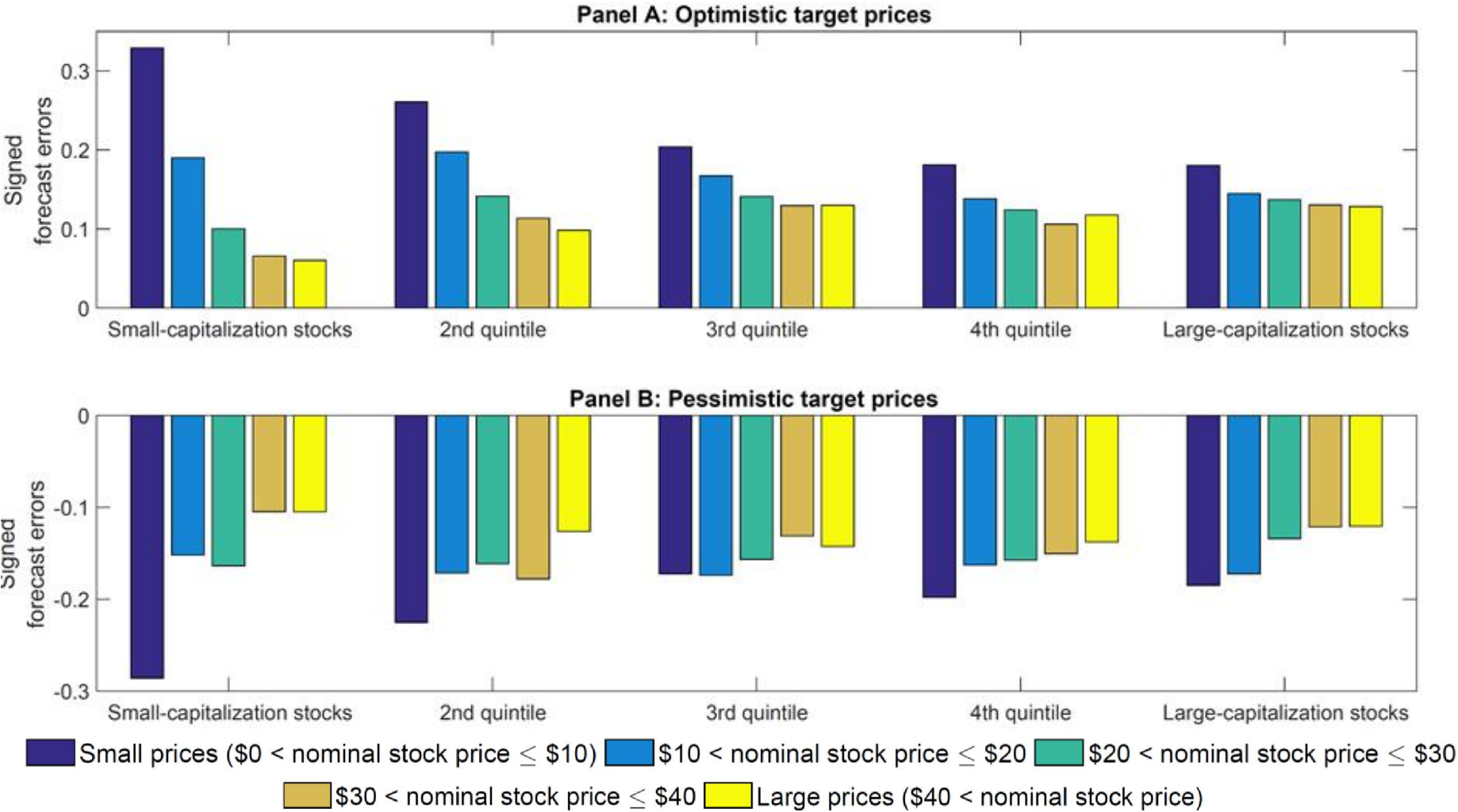
Univariate analysis

□ Average implied returns



Univariate analysis

Signed forecast errors



Multivariate analysis

- The premium in implied returns observed for small price stocks may be explained by risk factors, firms' characteristics and analysts' characteristics
- Fama MacBeth (1973) approach
 - As in Brav *et al.* (2005), Barber *et al.* (2013)

$$\begin{aligned}
 IR_{i,j,t} = & \alpha_t + \beta_{1,t}SIZE_{j,t} + \beta_{2,t}MOM_{j,t} + \beta_{3,t}BTM_{j,t} + NegativeIR_{i,j,t} \\
 & + \sum_{k=1}^4 \gamma_{k,t}PRICE_CAT_{j,t}^k + NegativeIR_{i,j,t} \times \sum_{k=1}^4 \theta_{k,t}PRICE_CAT_{j,t}^k \\
 & + \zeta_{i,t}AFE_{i,t} + \eta_{j,t}IFE_{j,t} + \delta_t Firm-Controls_{j,t} + \epsilon_{i,j,t}
 \end{aligned}$$

Optimistic target prices

Pessimistic target prices

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- Fama MacBeth (1973) approach
 - We therefore have 168 (14 years) cross-sectional regressions
 - We report the average of the estimated intercept and slope coefficients
 - Standard errors are adjusted using the Newey-West procedure

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Multivariate analysis

- Fama MacBeth (1973) approach
 - Controls
 - Operating profitability and investments
 - Fama and French (2015)
 - Dividend yield
 - Conflicts of interest
 - Distressed firms
 - 52-week high
 - Lottery-type stocks
 - LIDX index of Kumar, Page and Spalt (2016)
 - Skewness

Regression of target prices' implied returns on firm characteristics

	Model 1		Model 2		Model 3	
	Coefficient	Standard error	Coefficient	Standard error	Coefficient	Standard error
Intercept	0.4199***	0.0271				
Negative IR	-0.2638***	0.0134	-0.2215***	0.0104	-0.2220***	0.0097
\$0 to \$10 dummy	0.1956***	0.0134	0.1560***	0.0109	0.0981***	0.0053
\$10 to \$20 dummy	0.0736***	0.0092	0.0637***	0.0065	0.0355***	0.0039
\$20 to \$30 dummy	0.0314***	0.0046	0.0301***	0.0035	0.0175***	0.0031
\$30 to \$40 dummy	0.0114***	0.0032	0.0141***	0.0025	0.0089***	0.0023
\$0 to \$10 dummy × Negative IR	-0.2429***	0.0129	-0.1963***	0.0082	-0.2008***	0.0086
\$10 to \$20 dummy × Negative IR	-0.1016***	0.0085	-0.0813***	0.0048	-0.0959***	0.0050
\$20 to \$30 dummy × Negative IR	-0.0481***	0.0035	-0.0379***	0.0023	-0.0512***	0.0044
\$30 to \$40 dummy × Negative IR	-0.0179***	0.0030	-0.0131***	0.0029	-0.0192***	0.0039
Size	-0.0110***	0.0008	-0.0063***	0.0012	0.0010	0.0012
Book-to-market	-0.0216***	0.0037	-0.0078***	0.0018	-0.0048***	0.0017
Momentum	-0.0110*	0.0061	-0.0170***	0.0047	0.0163***	0.0027
Operating profitability					-0.0027**	0.0012
Investment					0.0038***	0.0012
Dividend Yield					-0.6962***	0.1143
External financing					0.0455***	0.0068
Earnings management					0.0011	0.0020
Negative earnings dummy					0.0262***	0.0000
52 week high ratio					-0.2435***	0.0200
LIDX					0.0513***	0.0100
Skewness					-0.0040***	0.0000
Industry fixed effects		NO		YES		YES
Analyst fixed effects		NO		YES		YES
Average adjusted R^2		32.81%		70.59%		75.05%
Number of observations		761,271		761,271		490,733

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Momentum	-0.0110*	0.0061

Regression of target prices' implied returns on firm characteristics

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\$10 to \$20 dummy × Negative IR	-0.1016***	0.0085	-0.0813***	0.0048	-0.0959***	0.0050
\$20 to \$30 dummy × Negative IR	-0.0481***	0.0035	-0.0379***	0.0023	-0.0512***	0.0044
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Book-to-market	-0.0216***	0.0037	-0.0078***	0.0018	-0.0048***	0.0017
Momentum	-0.0110*	0.0061	-0.0170***	0.0047	0.0163***	0.0027
Operating profitability					-0.0027**	0.0012
Investment					0.0038***	0.0012
Dividend Yield					-0.6962***	0.1143
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Skewness					-0.0040***	0.0000
Industry fixed effects		NO		YES		YES
Analyst fixed effects		NO		YES		YES
Average adjusted R^2		32.81%		70.59%		75.05%
Number of observations		761,271		761,271		490,733

	Model 2	
	Coefficient	Standard error
Intercept		
Negative IR	-0.2215***	0.0104
\$0 to \$10 dummy	0.1560***	0.0109
\$10 to \$20 dummy	0.0637***	0.0065
\$20 to \$30 dummy	0.0301***	0.0035
\$30 to \$40 dummy	0.0141***	0.0025
\$0 to \$10 dummy × Negative IR	-0.1963***	0.0082
\$10 to \$20 dummy × Negative IR	-0.0813***	0.0048
\$20 to \$30 dummy × Negative IR	-0.0379***	0.0023
\$30 to \$40 dummy × Negative IR	-0.0131***	0.0029
Size	-0.0063***	0.0012
Book-to-market	-0.0078***	0.0018
Momentum	-0.0170***	0.0047

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Momentum	-0.0110*	0.0061	-0.0170***	0.0047	0.0163***	0.0027
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Skewness					-0.0040***	0.0000
Industry fixed effects	NO		YES		YES	
Analyst fixed effects	NO		YES		YES	
Average adjusted R^2	32.81%		70.59%		75.05%	
Number of observations	761,271		761,271		490,733	

	Model 3	
	Coefficient	Standard error
Intercept		
Negative IR	-0.2220***	0.0097
\$0 to \$10 dummy	0.0981***	0.0053
\$10 to \$20 dummy	0.0355***	0.0039
\$20 to \$30 dummy	0.0175***	0.0031
\$30 to \$40 dummy	0.0089***	0.0023
\$0 to \$10 dummy \times Negative IR	-0.2008***	0.0086
\$10 to \$20 dummy \times Negative IR	-0.0959***	0.0050
\$20 to \$30 dummy \times Negative IR	-0.0512***	0.0044
\$30 to \$40 dummy \times Negative IR	-0.0192***	0.0039
Size	0.0010	0.0012
Book-to-market	-0.0048***	0.0017
Momentum	0.0163***	0.0027

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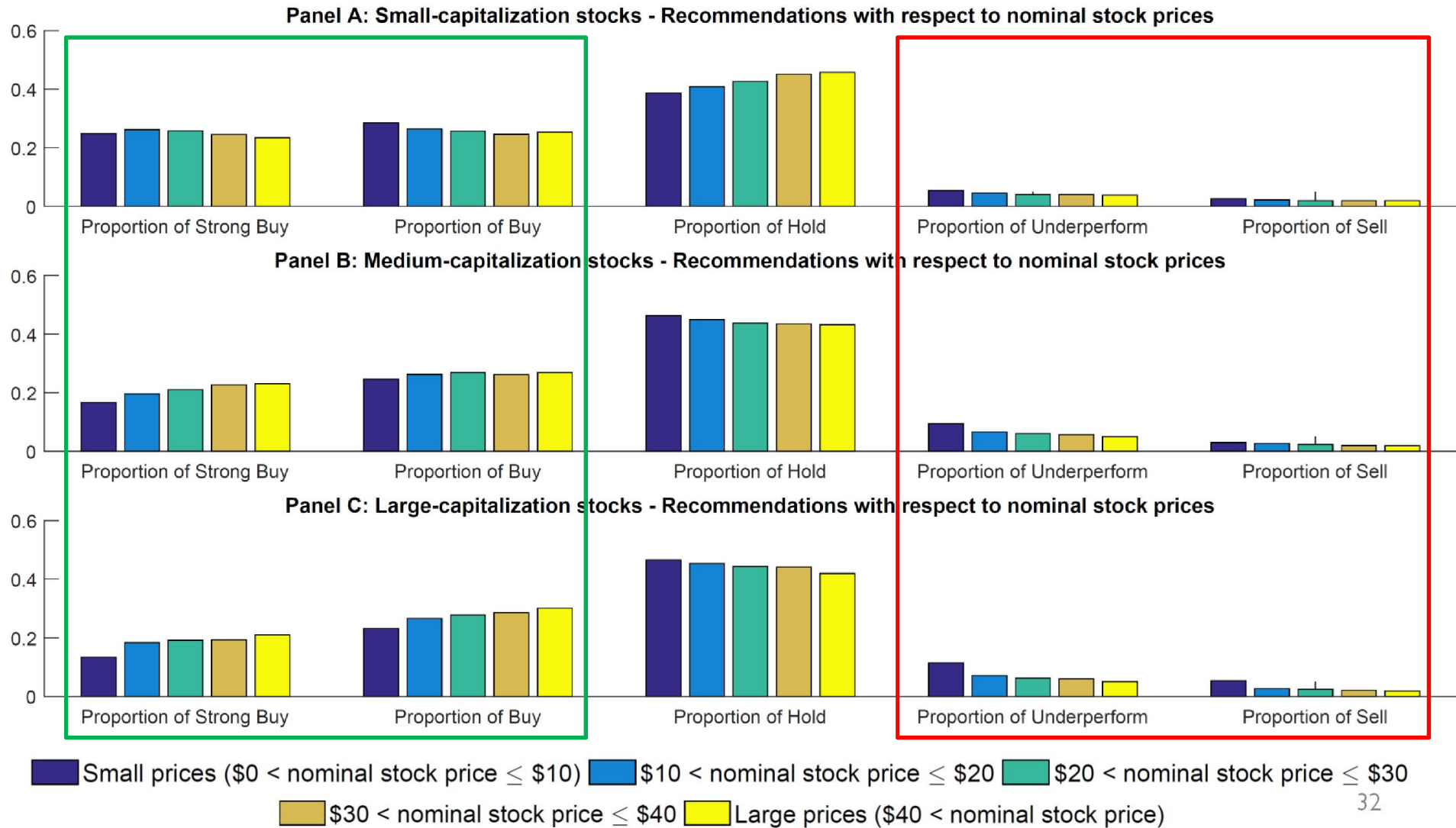
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- Risk adjusted returns and stock prices
 - ❑ Analysts' forecast higher risk-adjusted returns for small price stocks
 - ❑ Thus, analysts should make more favorable recommendations for small price stocks
 - ❑ Except if the differences in implied returns are the result of a behavioral bias
 - ❑ What happens when we look at recommendations?
 - Double sort on market capitalization and nominal prices

Recommendations



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Stock splits

- **Stock splits**
 - ❑ We look at implied returns pre-split and post-split (with a 3-month window around the split date)
 - ❑ Using stock splits allows us to make sure that the relationship between nominal prices and implied returns is not driven by other factors
 - ❑ We have
 - 532 splits with a ratio between 1.25 and 2
 - 869 splits with a ratio larger or equal to 2

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- ❑ For splits with ratio between 1.25 and 2:
 - Pre-split implied return of 15.78%
 - Post-split implied return of 20.30%
- ❑ For splits with ratio larger or equal to 2:
 - Pre-split implied return of 16.83%
 - Post-split implied return of 22.81%
- ❑ The differences are highly significant

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- Propensity score matching approach (Rosenbaum and Rubin, 1983)
 - We build a sample of controls firms with the same propensity to split as our splitting firms
 - We match on the following characteristics
 - Log price
 - Market capitalization
 - Previous return
 - Previous volatility
 - Book-to-market
 - Average previous implied return

Stock splits

□ Difference-in-differences analysis

	Average implied return		
	Splitting firms	Control firms	Difference
Split ratio between 1.25 and 2			
Before splits	0.1447	0.1845	-0.0398
After splits	0.1853	0.1927	-0.0074
Difference	0.0406	0.0082	0.0324***
Split ratio greater or equal to 2			
Before splits	0.1565	0.1879	-0.0314
After splits	0.2031	0.2019	0.0013
Difference	0.0466	0.0140	0.0326***

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- Nominal prices and implied returns
 - We provide strong evidence of a behavioral bias which
 - Leads analysts to be more optimistic on small price stocks
- Consequences for the research on analysts
 - Target prices issued on small price stocks are not accurate and are overoptimistic.

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● Other implications

- If educated professionals such as financial analysts suffer from this small price bias, other market participants may suffer from it as well.
- This small price bias may be the explanation for puzzles such as
 - Abnormal returns of small price stocks
 - Bandi, Russell and Sabbagui (2009), Birru-Wang(JFE 2016)
 - Higher volatility of small price stocks
 - Stock return comovements driven by price level
 - Green and Hwang (JFE 2009)
 - Abnormal returns following splits

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● Additional evidence

- ❑ *Another law of small numbers: Patterns of trading prices in experimental markets*
 - Roger T., Bousselmi W., Roger P. and M. Willinger
- ❑ Experimental markets
 - Small price markets and large price markets
 - Greater deviation from fundamental value in small price markets than in large price markets
 - Results are found between-participants and within-participants